

# Released Items

Student Name: Key

## NC Math 2



## 2017–2018



Public Schools of North Carolina  
State Board of Education  
Department of Public Instruction  
Raleigh, North Carolina 27699-6314

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# NC Final Exam



1 Which expression is equivalent to  $(8w^7x^{-5}y^3z^{-9})^{\frac{2}{3}}$ ?

A  $\frac{x^{\frac{10}{3}}z^6}{4w^{\frac{14}{3}}y^2}$

B  $\frac{4w^{\frac{14}{3}}y^2}{x^{\frac{10}{3}}z^6}$

C  $\frac{2w^{\frac{5}{3}}y^{\frac{1}{3}}}{x^{\frac{7}{3}}z^{\frac{11}{3}}}$

D  $\frac{x^{\frac{7}{3}}z^{\frac{11}{3}}}{2w^{\frac{5}{3}}y^{\frac{1}{3}}}$

Handwritten work for Question 1:

$(8w^7x^{-5}y^3z^{-9})^{\frac{2}{3}}$

Annotations: "negative exponents move to bottom", "put in calc", "8", "w", "x", "y", "z", "-2/3", "-14/3", "10/3", "-2", "6".

$$\frac{1 \cdot x^{\frac{10}{3}} z^6}{4 w^{\frac{14}{3}} y^2}$$

2 A marathon is roughly  $\overset{=d}{26.2}$  miles long. Which equation could be used to determine the time,  $t$ , it takes to run a marathon as a function of the average speed,  $s$ , of the runner where  $t$  is in hours and  $s$  is in miles per hour?

A  $t = 26.2 - 26.2s$

B  $t = 26.2 - \frac{s}{26.2}$

C  $t = 26.2s$

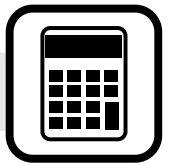
D  $t = \frac{26.2}{s}$

Handwritten work for Question 2:

$t(s) = \left(\frac{d}{s}\right)t$  solve for  $t$

$\frac{ts}{s} = \frac{d}{s}$

$t = \frac{d}{s}$        $t = \frac{26.2}{s}$



3 The force,  $F$ , acting on a charged object varies inversely to the square of its distance,  $r$ , from another charged object. When the two objects are 0.64 meter apart, the force acting on them is 8.2 Newtons. **Approximately** how much force would the object feel if it is at a distance of 0.77 meter from the other object?

$$y = \frac{k}{x}$$

- A 1.7 Newtons
- B 5.7 Newtons
- C 11.9 Newtons
- D 12.9 Newtons

$$F = \frac{k}{r^2}$$

$$F = \frac{3.36}{r^2}$$

$$F = \frac{3.36}{(.77)^2}$$

$$k \approx 3.36$$

$$F \approx 5.66$$

4 A system of equations is shown below.

$$y = x^2 + 2x + 8$$

$$y = -4x$$

plug x's into  $\rightarrow$  set equal to each other

What is the smallest value of  $y$  in the solution set of the system?

- A -4
- B -2
- C 8
- D 16

$$x^2 + 2x + 8 = -4x$$

$$x^2 + 6x + 8 = 0$$

$$4 \quad 8 \quad 2 \rightarrow \text{change signs}$$

$$6$$

$$x = -4 \quad y = -4(-4) = 16$$

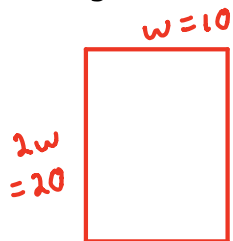
$$x = -2 \quad y = -4(-2) = 8$$



- 5 The cost of a newspaper advertisement is a function of its size.
- A company wants its advertisement to have a height that is twice its width.
  - The newspaper charges a flat rate of \$50 plus an additional \$10 per square inch.  $10x + 50$
  - The company can spend no more than \$2,050 on the advertisement.

What is the maximum height of an advertisement that the company can afford?

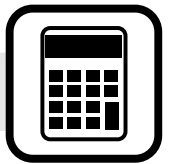
- A 5 inches
- B 10 inches
- C 15 inches
- D 20 inches



$$\begin{aligned}
 10x + 50 &= 2050 \\
 -50 &\quad -50 \\
 \hline
 10x &= 2000 \\
 \frac{10x}{10} &= \frac{2000}{10} \\
 x &= 200
 \end{aligned}$$

$$\begin{aligned}
 2w(w) &= 200 \\
 \frac{2w^2}{2} &= \frac{200}{2} \\
 \sqrt{w^2} &= \sqrt{100} \\
 w &= 10
 \end{aligned}$$

RELEASED



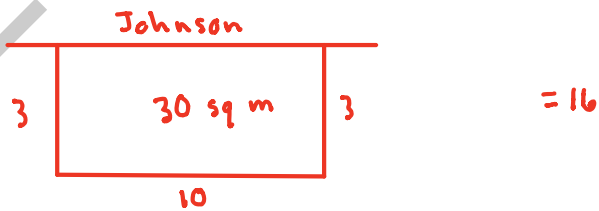
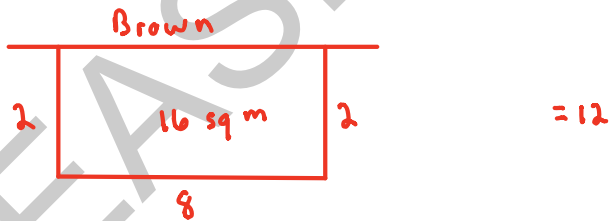
- 6 Farmer Brown built a rectangular pen for his chickens using 12 meters of fence.
- He used part of one side of his barn as one length of the rectangular pen.
  - He maximized the area using the 12 meters of fence.

Farmer Johnson built a rectangular pen for her chickens using 16 meters of fence.

- She used part of one side of her barn as one length of the rectangular pen.
- The length of her pen was 2 meters more than the length of Farmer Brown's pen.
- The width of her pen was 1 meter more than the width of Farmer Brown's pen.

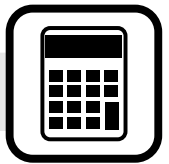
How much larger is Farmer Johnson's rectangular pen than Farmer Brown's?

- A 24 square meters
- B 18 square meters
- C 16 square meters
- D 14 square meters



$$30 - 16 = 14 \text{ sq meters more}$$

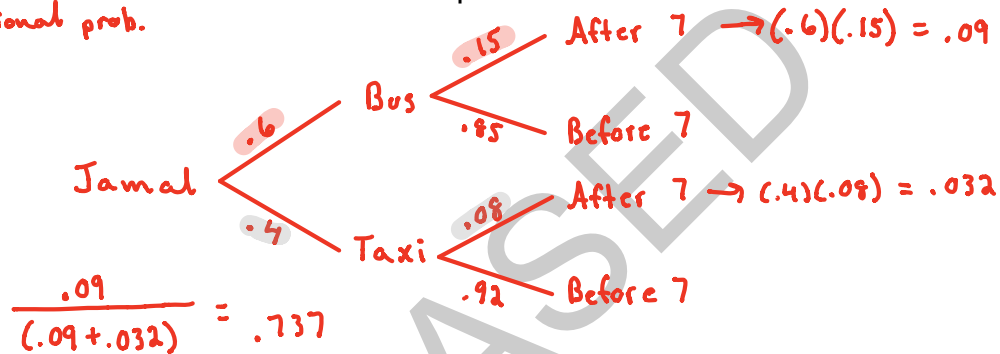
J   B



- 7 Suppose that Jamal can choose to get home from work by taxi or bus.
- When he chooses to get home by taxi, he arrives home after 7 p.m. 8 percent of the time. *Before 7pm → 92%*
  - When he chooses to get home by bus, he arrives home after 7 p.m. 15 percent of the time. *Before 7pm → 85%*
  - Because the bus is cheaper, he uses the bus 60 percent of the time. *Taxi → 40%*

What is the **approximate** probability that Jamal chose to get home from work by bus, given that he arrived home after 7 p.m.?

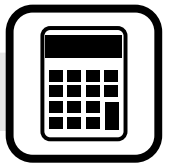
- conditional prob.*
- ~~A~~ 0.09
  - ~~B~~ 0.14
  - ~~C~~ 0.60
  - D 0.74



- 8 The graph of  $f(x) = 2x^2 - 3x + 5$  will be translated 8 units down, producing the graph of  $q(x)$ . Which equation represents the new function,  $q(x)$ ?

- A  $q(x) = 2x^2 - 3x - 3$
- ~~B~~  $q(x) = 2x^2 - 11x + 5$
- ~~C~~  $q(x) = 2x^2 - 3x + 13$
- ~~D~~  $q(x) = 2x^2 + 5x + 5$

$$\begin{array}{r} 2x^2 - 3x + 5 \\ - 8 \\ \hline 2x^2 - 3x - 3 \end{array}$$



9 The equation  $2x^2 - 5x = -12$  is rewritten in the form of  $2(x - p)^2 + q = 0$ . What is the value of  $q$ ?

A  $\frac{167}{16}$

B  $\frac{71}{8}$

C  $\frac{25}{8}$

D  $\frac{25}{16}$

$$\left(\frac{-5}{2}\right)^2$$

$$\left(\frac{-5}{4}\right)^2$$

$$\frac{25}{16}$$

$2x^2 - 5x = -12$   
 $2\left(x^2 - \frac{5}{2}x + \frac{25}{16}\right) = -12 + 2\left(\frac{25}{16}\right)$

*multiply by 2 because it was pulled out*

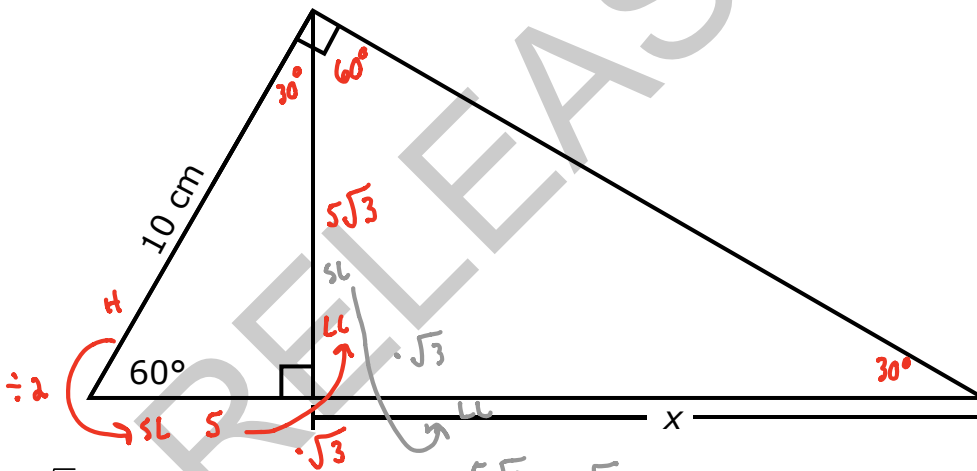
$2\left(x - \frac{5}{4}\right)^2 = -\frac{71}{8}$

$$\frac{+71}{8} \quad \frac{+71}{8}$$

$$2\left(x - \frac{5}{4}\right)^2 + \frac{71}{8} = 0$$

*P*      *q*

10 What is the value of  $x$  in the triangle below?



A  $\frac{5\sqrt{3}}{2}$  cm

B  $5\sqrt{3}$  cm

C 10 cm

D 15 cm

$5\sqrt{3} \cdot \sqrt{3}$   
 $5 \cdot 3$   
 $= 15$



- 11 The length of a rectangular prism is  $4\sqrt{3}$  units. The height is  $3\sqrt{6}$  units. If the volume is irrational, which could be the measure of the width of the rectangular prism? *↳ has radical in it*

A  $2\sqrt{50}$   
 B  $4\sqrt{12}$   
 C  $5\sqrt{8}$   
 D  $7\sqrt{18}$

$V = l \cdot w \cdot h$   
 $V = (4\sqrt{3})(3\sqrt{6}) \cdot w$   
 $V = 12\sqrt{18} \cdot w$   
*simplify*  
 $V = 36\sqrt{2} \cdot w$

When the 2 under the radical is multiplied by the highlighted #'s, they create a perfect square #.

- 12 Which function is equivalent to  $y = x^2 - 6x + 10$ ?

A  $y = (x + 3)^2 - 1$   
 B  $y = (x - 3)^2 + 1$   
 C  $y = (x + 6)^2 - 10$   
 D  $y = (x - 6)^2 + 10$

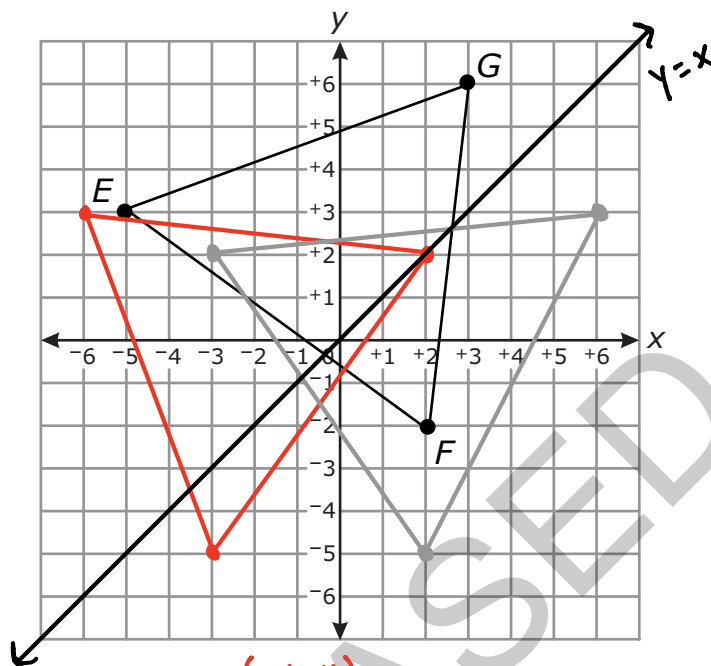
$y - 10 \xrightarrow{-10} = x^2 - 6x \xrightarrow{-10} + 9$   
 $y - 10 + 9 = x^2 - 6x + 9$   
 $y - 1 = (x - 3)^2$   
 $y = (x - 3)^2 + 1$

$\left(\frac{-6}{2}\right)^2$   
 $\downarrow$   
 $(-3)^2$   
 $\downarrow$   
 $9$



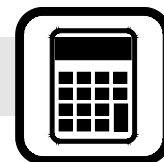


13 Triangle  $EGF$  is graphed below.



Triangle  $EGF$  will be rotated  $90^\circ$  counterclockwise around the origin and will then be reflected across the  $y$ -axis, producing an image triangle. Which additional transformation will map the image triangle back onto the original triangle?

- A rotation  $270^\circ$  counterclockwise around the origin
- B rotation  $180^\circ$  counterclockwise around the origin
- C reflection across the line  $y = -x$
- D reflection across the line  $y = x$



**NC Math 2  
RELEASED Items<sup>1</sup>  
2017–2018  
Answer Key**

<b>Item Number</b>	<b>Type<sup>2</sup></b>	<b>Key</b>	<b>Percent Correct<sup>3</sup></b>	<b>Standard</b>
1	MC	A	37%	N-RN.2
2	MC	D	67%	A-CED.2
3	MC	B	40%	A-REI.2
4	MC	C	33%	A-REI.7
5	MC	D	47%	F-IF.8
6	MC	D	35%	F-BF.1
7	MC	D	20%	S-CP.6
8	MC	A	61%	F-BF.3
9	MC	B	30%	A-REI.4a
10	MC	D	61%	G-SRT.8
11	MC	B	46%	N-RN.3
12	MC	B	67%	A-SSE.3
13	MC	D	23%	G-CO.5