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1. For each of the following functions, state the equation of the base function, the transformations from the base function, the domain, range, asymptotes. If the function is exponential, determine if it is a growth or decay model. Then graph each function.

2. Use the rules of exponents and/or logarithms to find the value of $x$ in each equation. Round to the nearest hundredth when necessary.
a. $\quad\left(3^{2 x}\right)\left(3^{12}\right)=3^{20}$
b. $\frac{5^{8}}{5^{2 x}}=5^{10}$
c. $\left(13^{4}\right)^{x}=13^{24}$
d. $\left(25^{2 x}\right)\left(5^{7}\right)=125^{4}$
e. $\frac{9^{5 x}}{3^{2 x}}=81^{12}$
f. $\left(8^{4}\right)^{x}=4^{18}$
g. $\left(49^{2 x}\right)\left(7^{8}\right)=1$
h. $(25)^{\frac{1}{2}}(3)^{4}=x$
i. $\left(6^{\frac{1}{2}}\right)\left(36^{\frac{3}{2}}\right)=6^{x}$
j. $\quad 10^{x+4}=100,000,000$
k. $6(10)^{5 x}=18,000$
3. $10^{3 x-4}=1,000$
m. $10^{6 x}=80,000$
n. $8(10)^{2 x}+30=150$
o. $10^{4 x+7}=1$
p. $-5(10)^{x-9}=-5,000$
q. $\frac{1}{2}(10)^{2 x}=50,000$
r. $10^{2 x}=.0001$
s. $\quad \log (x+5)=2$
t. $\log _{3}(4 x-3)=4$
u. $\log _{x} 8=3$
v. $\log _{x} 144=2$
w. $\log _{4}(4 x)=3$
x. $\log (25 x)=2$
4. Find the inverse of each function
a. $y=\frac{1}{2} x-5$
b. $y=4 x^{2}$
c. $y=\sqrt[3]{x+4}$
5. Rewrite each function in exponential form. (2 points each)
a. $216=6^{x}$
b. $x=12^{6}$
c. $81=3^{8 x}$
6. Rewrite each function in logarithmic form. (2 points each)
a. $\quad \log _{3} 243=x$
b. $\log _{15} x=3$
d. $\log _{x} 120=3$
7. Suppose that 500 mg of a medicine enters a hospital patient's bloodstream at noon and decays exponentially at a rate of $15 \%$ per hour. The exponential function $D(t)=500\left(10^{-0.07 t}\right)$ models the amount of medicine active in the patient's blood at a time $t$ hours later, where $t$ is time in hours. Round answers to the nearest hundredth.
a. Find $\mathrm{D}(0)$.
b. Find $D(3)$.
c. Use logarithms to determine when there is 150 mg of medicine in the patient's blood stream.
d. Use logarithms to determine when there is 10 mg of medicine in the patient's blood stream.
8. The function $y=12,800(1.045)^{x}$ represents the value of a piece of artwork $x$ years after purchase.
a. How much will the artwork be worth in 15 years?
b. When will the artwork be worth $\$ 20,000$ ?
