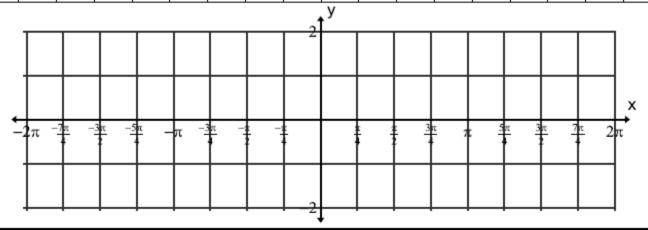
## Graphing Sine & Cosine

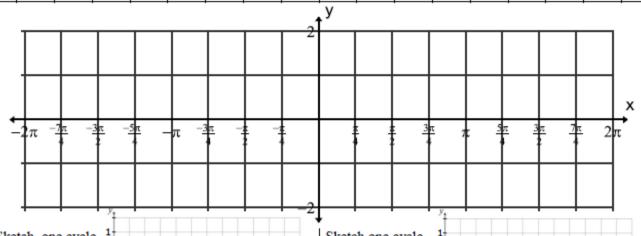
Fill in the table for  $f(x) = \sin(x)$  (round to the nearest thousandths).

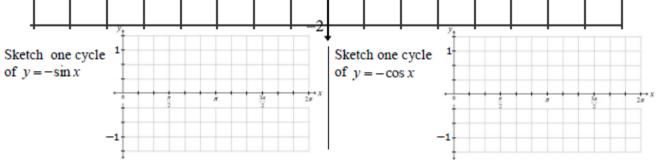
х	-2π	$-\frac{7\pi}{4}$	$-\frac{3\pi}{2}$	$-\frac{5\pi}{4}$	$-\pi$	$-\frac{3\pi}{4}$	$-\frac{\pi}{2}$	$-\frac{\pi}{4}$	0	$\frac{\pi}{4}$	$\frac{\pi}{2}$	$\frac{3\pi}{4}$	π	$\frac{5\pi}{4}$	$\frac{3\pi}{2}$	$\frac{7\pi}{4}$	2π
y																	



Fill in the table for  $f(x) = \cos(x)$  (round to the nearest thousandths).

х	-2n	$-\frac{7\pi}{4}$	$-\frac{3\pi}{2}$	$-\frac{5\pi}{4}$	-π	$-\frac{3\pi}{4}$	$-\frac{\pi}{2}$	$-\frac{\pi}{4}$	0	$\frac{\pi}{4}$	$\frac{\pi}{2}$	$\frac{3\pi}{4}$	π	$\frac{5\pi}{4}$	$\frac{3\pi}{2}$	$\frac{7\pi}{4}$	2π
у																	





From the graphing activity, you should have discovered that sine and cosine values repeat themselves. Thus, the sine and cosine functions are periodic.

A function is **periodic** if there is a positive number p such that f(t + p) = f(t) for every t. The least such positive number is called the **period**.

Points you should know from the unit circle

х	Angle in Radians	0	π/2	π	3π/2	2π
у	sin x					

**Sine Function:**  $y = \sin x$ 

- called a "wave" because of its rolling wave-like appearance (also referred to as oscillating)
- amplitude: 1 (height)
- period:  $2\pi$  (length of one cycle)
- frequency: 1 cycle in 2π radians [or 1/(2π)]
- domain:  $\{x | x \in \mathbb{R}\}$
- range:  $(y \mid -1 \leq y \leq 1)$

At x = 0, the sine wave is on the shoreline! (meaning the y-value is equal to zero)



<i>y</i> =	$= \sin x$		
/ `			
			×
π/2	π	3π/2	2π
			/
		$\bigvee$	
		$y = \sin x$	

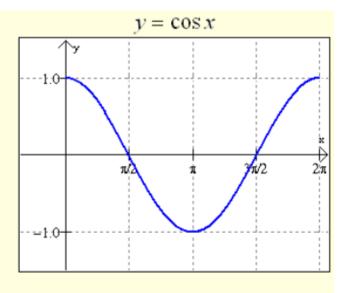
х	Angle in Radians	0	π/2	π	3π/2	2π
у	cos x					

**Cosine Function:**  $y = \cos x$ 

- called a "wave" because of its rolling wave-like appearance
- amplitude: 1
- period: 2π
- frequency: 1 cycle in  $2\pi$  radians [or  $1/(2\pi)$ ]
- domain:  $\{x | x \in \mathbb{R}\}$
- range:  $(y \mid -1 \leq y \leq 1)$

At x = 0, the cosine wave breaks off the cliff! (meaning the y-value is equal to one)

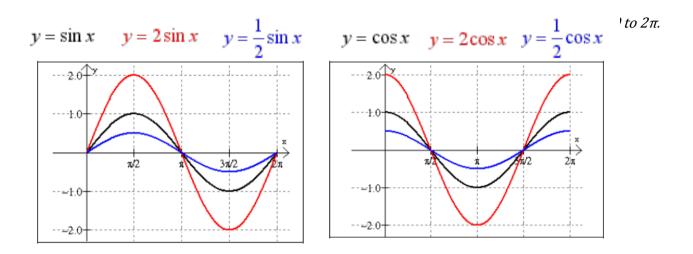




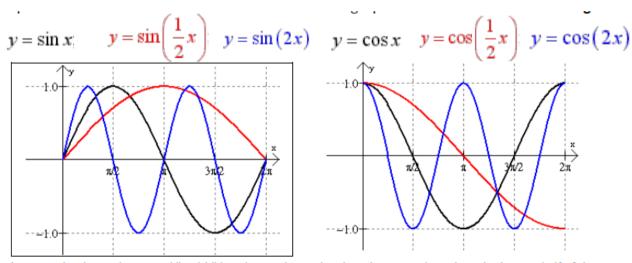
## Transformations of the sine and cosine graphs

$$y = a \sin(b(x - h)) + k$$
 and  $y = a \cos(b(x - h)) + k$ 

➤ The value **a** affects the amplitude. The **amplitude** (half the distance from the max to the min) will be |**a**| because distance is always positive. Increasing or decreasing an **a** value will *vertically stretch or shrink* a graph.

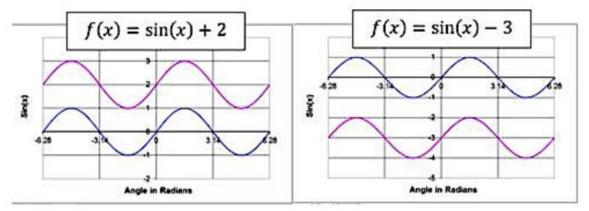


The **b** value is the number of cycles it completes in an interval of  $(0, 2\pi)$  or  $(0^{\circ}, 360^{\circ})$ . The **b** value affects the **period**. The period of sine and cosine is  $|\frac{2\pi}{b}|$ . When 0 < b < 1 the period of the function is greater than  $2\pi$  and the graph will have a *horizontal stretch*. When **b**>1, the period is less than  $2\pi$  and the graph will have a *horizontal shrink*.



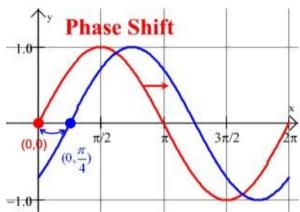
These graphs change horizontal "width" but do not change height. The two red graphs only show us half of the original graphs in their 0 to  $2\pi$  windows. We would need to "stretch" the domain window to  $4\pi$  to see entire cycles of those two graphs. The two blue graphs show us two complete cycles of the graphs in their 0 to  $2\pi$  windows, which would allow us to "shrink" the domain window and still see complete cycles of the graphs.

➤ Just like any other function, adding a constant **on the end of the function** will shift the trig graph vertically (up if the constant is *positive*, down if the constant is *negative*).



The vertical change is called the <u>midline</u>. It is always y = k

Also just like any other function, adding a constant on **into the function** will shift the trig graph *horizontally* (left if the constant is positive, right if the constant is negative). This is called a **phase shift**.



Note: You may have to factor out b in order to determine the phase shift or set what is inside main parentheses = 0 and solve for x.

Example: Determine midline, vertical shift, amplitude, period, and phase shift.

a) 
$$y = 2\sin\left(\frac{2}{3}x + \frac{\pi}{3}\right) - 1$$

**b)** 
$$y = 3\cos\left(\frac{1}{2}(x-2)\right) + 4$$