

Theoretical Probability of Events $P(E)$	$\frac{\text{what we want}}{\text{total possible outcomes}}$
$P(A^c)$	the complement of the successful event

Example: An experiment consists of **tossing three coins**. $2^3 = 8$ outcomes

- List the sample space for the outcomes of the experiment.

HHH THH TTH HHT HTT HTH THT TTT

Find the following probabilities:

2. $P(\text{all heads}) = \frac{1}{8}$

3. $P(\text{two tails}) = \frac{2}{8} = \frac{1}{4}$

4. $P(\text{no heads}) = \frac{1}{8}$

5. $P(\text{at least one tail}) = \frac{7}{8}$

6. How could you use complements to find #5? $P(\text{no heads}^c)$

“And” → Multiply

“OR” → Add
(sometimes subtract)

Example: A bag contains **six red marbles**, **four blue marbles**, **two yellow marbles** and **three white marbles**. One marble is drawn at random.

- List the sample space for this experiment.

RRRRRRBBBBYYWWW

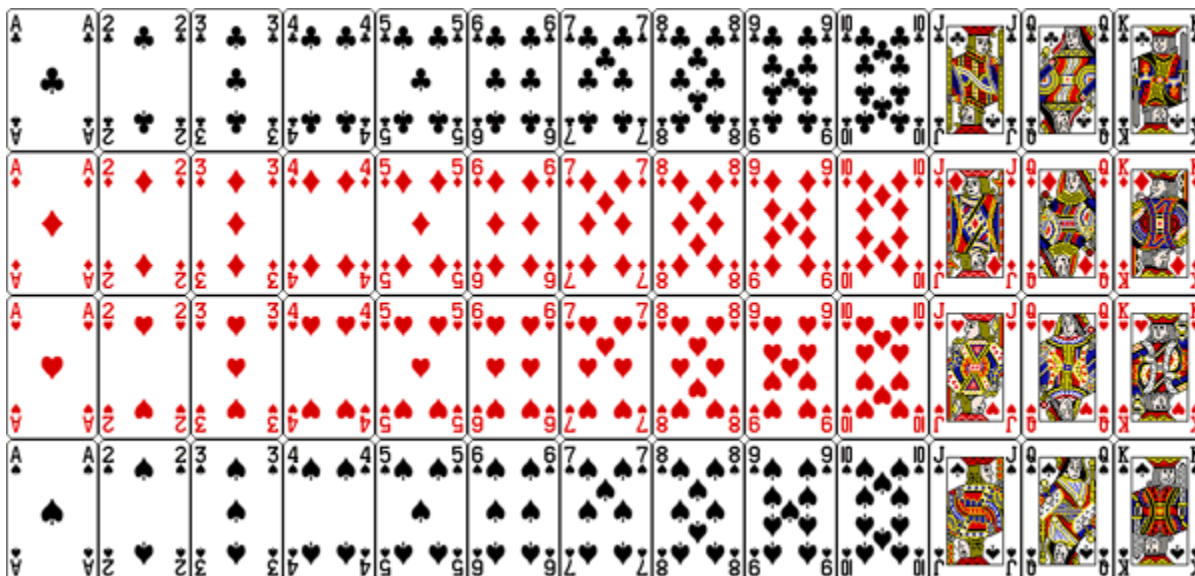
Find the following probabilities:

8. $P(\text{red}) = \frac{6}{15} = \frac{2}{5}$

9. $P(\text{blue or white}) = \frac{7}{15}$

10. $P(\text{not yellow}) = \frac{13}{15}$

Note that we could either count all the outcomes that are not yellow, or we could think of this as being $1 - P(\text{yellow})$. Why is this? *They are complements of each other*



Example: A card is drawn at random from a standard deck of cards. Find each of the following:

1. $P(\text{heart}) = \frac{13}{52} = \frac{1}{4}$
2. $P(\text{black card}) = \frac{26}{52} = \frac{1}{2}$
3. $P(2 \text{ or jack}) = \frac{8}{52} = \frac{2}{13}$
4. $P(\text{not a heart}) = \frac{39}{52} = \frac{3}{4}$

Example: Given the Venn Diagram below, find the probability of the following if a student was selected at random:

5. $P(\text{blonde hair}) = \frac{13}{26} = \frac{1}{2}$
6. $P(\text{blond hair and blue eyes}) = \frac{8}{26} = \frac{4}{13}$
7. $P(\text{blonde hair or blue eyes}) = \frac{21}{26}$
8. $P(\text{not blue eyes}) = \frac{16}{26} = \frac{8}{13}$

