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## Basic Counting Methods for Determining the Possible Outcomes

A. Fundamental Counting Principle:
a. Tree Diagrams:

Example \#1: Alpo manufactures 4 different types of dog food: puppy, adult, active and senior. Each type comes in two different sizes: 8 lbs or 16 lbs . Make a tree diagram representing the different products. How many different products can the company display?
b. In general:

- If there are $m$ ways to make a first selection and $n$ ways to make a second selection, then there are $m \bullet n$ ways to make the two selections simultaneously. This is called the Fundamental Counting Principle.

Example \#1 above: 4 different types of dog food in 2 different sizes. How many different products?

Example \#2: Joey has to pick out an outfit for school. He has 2 pairs of pants appropriate for school: one blue, one black. He has 3 shirts: one red, one green, one blue. He has 2 pairs of shoes to choose from: one blue, one black. How many different outfits can Joey select?

Example \#3 (more restricted) Telephone numbers, in US, begin with three-digit area codes followed by seven-digit local telephone numbers. How many different telephone numbers are possible? (Area codes and local telephone numbers cannot begin with 0 or 1)

Example \#4 In a certain state, automobile license plates display 3 letters followed by 3 digits. How many such plates are possible if repetition of the letters is
(a) allowed?
(b) not allowed?

Example \#5 In how many different ways can a race with six runners be completed? Assume there is no tie.

Example \#6 Three digit numbers are formed using the digits 2, 4, 5, and 7, with repetition of digits allowed. How many such numbers can be formed if
(a) the numbers are less than 700 ?
(b) the numbers are even?
(c) the numbers are divisible by 5 ?
(d) the number must start with a 2 ?

Example \#7 A senate subcommittee consists of ten Democrats and seven Republicans. In how many ways can a chairman, vice chairman, and secretary be chosen if
a) there are no restrictions?
b) the chairman must be a Democrat and the vice chairman must be a Republican?

1) There are 6 people in a race. In how many ways can they finish first, second or third?
2) A golfer has 4 different hats, 3 gloves and 2 pairs of shoes to pick from for his roumd of golf. In how many ways can he make his choices?
3) In Canada, postal codes consist of 6 characters - three letters and three digits. Each postal code starts with a letter and altemates with a digit.
a. How many postal codes are there ?
b. How many start with the letter $S$ ?
c. How many start with the letter $S$ and end in the digit 8 ?
d. How many start with the letter $S$. digit 6 and NO letter or digit is repeated?
4) Using the digits $\{1,2,3,4,5\}$, how many positive three digit integers can be made if:
a. there are NO restrictions
b. it is odd and repetition is allowed?
c. it is odd and repetition is NOT allowed ?
d. Repeat question $\mathrm{a}, \mathrm{b}$ and c if the digits you can choose are $\{0,1,2,3,4,5\}$.
5) In how many ways can ALL of the letters of the word TRAVEL be arranged if:
a. there are NO restrictions ?
b. it must start with $T$ ?
c. it starts with a consonant and ends in a vowel ?
d. the letters IR must stay together?
6) How many positive even three-digit integers less than 400 can be formed from the digits $\{0,1,2,3,4,5\}$ if:
a. repetition is allowed?
b. No digit is repeated?
7) You are ordering dimer at a restaurant. How many ways can you order a meal if you have two choices for a drink ( coffee or tea), three main courses to choose from ( chicken, beef, or fish) and two desserts (pie or cake)?
a. Draw a tree diagram
b. Use the fundamental counting principle
8) Eight sprinters are in the final of a race. How many different ways there to award the gold. silver and bronze medals?
9) Television stations in Canada usually have call letters that are 4 letters long and begin with the letter C. If the CRTC made this a law in Canada, then how many television stations could the CRTC license?
10) Repeat the above question using the restriction, repetition of letters is NOT allowed
11) Some license plates consist of 3 letters followed by 3 mumbers. How many different license plates are possible if
a. if there are NO Restrictions
b. if the letters must be DIFFERENT
c. if the letters are different and the first digit can't be 0
12) How many two digit whole mumbers can be formed using the digits: $0,1,2,4,6,7,8,9$ ( 8 digits)?
a. Repetitions are allowed
b. Repetitions are not allowed
13) An ice cream parior features 64 flavors and 20 toppings, in 3 sizes. How many different sundaes can be made ?
14) How many EVEN two digit numbers are there?
15) How many EVEN two digit numbers can be made using the digits $1,2,3,4,5,6,7,8$ ?
a. Repetitions are not allowed
b. Repetitions are allowed
16) How many two digit numbers can be formed using the digits $0,2,4,6,8$ if
a. Repetitions are allowed
b. Repetitions are not allowed
17) How many ODD four digit numbers can be made from all of the digits, if
a. Repetition is allowed
b. Repetition is not allowed
18) In how many ways can all of the letters of the word PROBLEM be arranged?
19) In how many ways can all of the letters of the word PROBLEM be arranged if the arrangement must start with a consonant and end in a vowel?
20)How many ways can the letters in the word PENCII be arranged?
20) If there are four different types of cookies, how many ways can you eat all of them?
22)If three albums are placed in a multi-disc stereo, how many ways can the albums be played?
21) How many ways can you order the letters in KEYBOARD if K and Y must always be kept together?
22) How many ways can the letters in OBTUSE be ordered if all the vowels must be kept together?
23) How many ways can 4 rock, 5 pop, \& 6 classical albums be ordered if all albums of the same gerre must be kept together?
